**Hampshire Mathematics Team Assessment Model - Fluency, Reasoning and Problem Solving** Version 4: November 2015

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| **Year****4** | **Number and place value** | **Addition and subtraction** | **Multiplication and division** | **Fractions** | **Measurement** | **Geometry** |
| **Properties of shape** | **Position and****direction** |
| **Fluency Reasoning****Problem solving** | solve number and practical problems that involve all of the above and with increasingly large positive numbers | solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why**Statistics*** solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs.
 | solve problems involving multiplying and adding using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects. | * Solve problems involving increasingly harder factions to calculate quantities, and fractions to divide quantities,
* including non-unit fractions where the answer is a whole number
* solve simple measure and money problems involving fractions and decimals to two decimal places
 | solve problems involvingconverting from hours to minutes; minutes to seconds; years to months; weeks to days**Statistics*** solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs.
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| **Phase 1 inc Year 3** | * Count in multiples of 25 and 1000
* find 1000 more or less than a given number
* recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones)
* identify, represent and estimate numbers using different representations
* round any number to the nearest 10, 100
 | * estimate and use inverse operations to check answers to a calculation

**Statistics*** statistics: interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs
 | * use place value, known and derived facts to multiply and divide mentally
 | * recognise and show, using diagrams
* find the effect of dividing a one- or two-digit number by 10 and 100
* add and subtract fractions with the same denominator
* round decimals with one decimal place to the nearest whole number
 | * measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres
* estimate, compare and calculate different measures, including money in pounds and pence

**Statistics*** statistics: interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs
 |  compare and classify geometric shapes**,** based on their properties and sizes identify acute and obtuse angles complete a simple symmetric figure with respect to a specific line of symmetry | * describe positions on a 2-D grid as coordinates in the first quadrant
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|  | **Phase 2** | * Count in multiples **of 6**, 25 and 1000
* count backwards through zero to include negative numbers
* order and compare numbers beyond 1000
* round any number to the nearest 10, 100 **or 1000**
 | * add and subtract numbers with up to 4 digits
 | * recall 2/3/4/5/6/8 multiplication and division facts for multiplication tables
* use place value, known and derived facts to multiply and divide mentally, **including:**
	+ **multiplying by 0 and 1**
	+ multiply two-digit and three-digit numbers by a one-digit number
 | * recognise and show, using diagrams, **families of common equivalent fractions**
* recognise that hundredths arise when dividing an object by a hundred and dividing tenths by ten.
* find the effect of dividing a one- or two-digit number by 10 and 100**, identifying the value of the digits in the answer as** **ones, tenths**
* solve simple measure and money problems involving fractions
 | * **estimate, compare and calculate different measures,** including money in pounds and pence
* read, write and convert time between analogue and digital 12 and 24-hour clocks
 | * compare and classify geometric shapes, including **quadrilaterals** based on their properties and sizes
* identify lines of symmetry in 2-D shapes presented in different orientations
 | * describe movements between positions as translations of a given unit to the left/right and up/ down
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|  |  | **Phase 3** | * read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value.
 | * add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate
 | * multiplication and division facts for multiplication tables **up to 12 × 12**
* use place value, known and derived facts to multiply and divide mentally,
* including: multiplying by 0 and 1; **dividing by 1; multiplying together three numbers**
* recognise and use factor pairs and
* commutativity in mental calculations
* multiply two-digit and three-digit numbers by a one-digit number **using formal written layout**
* using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects.
 | * count up and down in hundredths
* recognise and write decimal equivalents of any number of tenths or hundredths
* recognise and write decimal equivalents to 1/4; 1/2; 3/4
* identifying the value of the digits in the answer as ones, tenths **and hundredths**
* compare numbers with the same number of decimal places up to two decimal places
* solve simple measure and money problems involving fractions **and decimals to two decimal places.**
 | * solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days.
* estimate, compare and calculate different measures, including money in pounds and pence (repeat from Phase 1, 2 deeper level)
 | * compare and classify geometric shapes, including quadrilaterals **and triangles,** based on their properties and sizes
* identify acute and obtuse angles **and compare and order angles up to two right angles by size**
 | * plot specified points and draw sides to complete a given polygon
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Mathematics Programme of study key stage 1 and 2 September 2013 Notes and Guidance (non-statutory)

**Lower Key Stage 1 Years 3 and 4**

The principal focus of mathematics teaching in lower key stage 2 is to ensure that pupils become increasingly fluent with whole numbers and the four operations, including number facts and the concept of place value. This should ensure that pupils develop efficient written and mental methods and perform calculations accurately with increasingly large whole numbers.

At this stage, pupils should develop their ability to solve a range of problems, including with simple fractions and decimal place value. Teaching should also ensure that pupils draw with increasing accuracy and develop mathematical reasoning so they can analyse shapes and their proper- ties, and confidently describe the relationships between them. It should ensure that they can use measuring instruments with accuracy and make connections between measure and number.

By the end of year 4, pupils should have memorised their multiplication tables up to and including the 12 multiplication table and show precision and fluency in their work.

Pupils should read and spell mathematical vocabulary correctly and confidently, using their growing word reading knowledge and their knowledge of spelling.

**Year 4**

**Number and place value**

Using a variety of representations, including measures, pupils become fluent in the order and place value of numbers beyond 1000, including counting in tens and hundreds, and maintaining fluency in other multiples through varied and frequent practice. They begin to extend their knowledge of the number system to include the decimal numbers and fractions that they have met so far.

They connect estimation and rounding numbers to the use of measuring instruments.

Roman numerals should be put in their historical context so pupils understand that there have been different ways to write whole numbers and that the important concepts of zero and place value were introduced over a period of time.

**Addition and subtraction**

Pupils continue to practise both mental methods and columnar addition and subtraction with increasingly large numbers to aid fluency (see Mat hemati c s Ap pe ndi x 1 ).

**Multiplication and division**

Pupils continue to practise recalling and using multiplication tables and related division facts to aid fluency.

Pupils practise mental methods and extend this to three-digit numbers to derive facts, (for example 600 ÷ 3 = 200 can be derived from 2 x 3 = 6).

Pupils practise to become fluent in the formal written method of short multiplication and short division with exact answers (see Mat hemati c s Ap pen dix 1 ).

Pupils write statements about the equality of expressions (for example, use the distributive law 39 × 7 = 30 × 7 + 9 × 7 and associative law (2 × 3) × 4 = 2 × (3 × 4)). They combine their knowledge of number facts and rules of arithmetic to solve mental and written calculations for example, 2 x 6 x 5 = 10 x 6

= 60.

Pupils solve two-step problems in contexts, choosing the appropriate operation, working with increasingly harder numbers. This should include correspondence questions such as the numbers of choices of a meal on a menu, or three cakes shared equally between 10 children.

**Fractions**

Pupils should be taught to:

recognise and show, using diagrams, families of common equivalent fractions

count up and down in hundredths; recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten.

solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole numbe add and subtract fractions with the same denominator

recognise and write decimal equivalents of any number of tenths or hundredths

recognise and write decimal equivalents to ¼, ½ , ¾

find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths

round decimals with one decimal place to the nearest whole number

compare numbers with the same number of decimal places up to two decimal places

solve simple measure and money problems involving fractions and decimals to two decimal places.

Pupils should connect hundredths to tenths and place value and decimal measure. They extend the use of the number line to connect fractions, numbers and measures.

Pupils understand the relation between non-unit fractions and multiplication and division of quantities, with particular emphasis on tenths and hundredths.

Pupils make connections between fractions of a length, of a shape and as a representation of one whole or set of quantities. Pupils use factors and multiples to recognise equivalent fractions and simplify where appropriate (for example, 6/8 = 2/3 or 1/4=2/8 ). Pupils continue to practise adding and subtracting fractions with the same denominator, to become fluent through a variety of increasingly complex problems beyond one whole.

Pupils are taught throughout that decimals and fractions are different ways of expressing numbers and proportions.

Pupils’ understanding of the number system and decimal place value is extended at this stage to tenths and then hundredths. This includes relating the decimal notation to division of whole number by 10 and later 100.

They practise counting using simple fractions and decimals, both forwards and backwards.

Pupils learn decimal notation and the language associated with it, including in the context of measurements. They make comparisons and order decimal amounts and quantities that are expressed to the same number of decimal places. They should be able to represent numbers with one or two decimal places in several ways, such as on number lines.

**Measurement**

Pupils build on their understanding of place value and decimal notation to record metric measures, including money. They use multiplication to convert from larger to smaller units.

Perimeter can be expressed algebraically as 2(*a* + *b*) where a and b are the dimensions in the same unit. They relate area to arrays and multiplication.

**Geometry- properties of shapes**

Pupils continue to classify shapes using geometrical properties, extending to classifying different triangles (for example, isosceles, equilateral, scalene) and quadrilaterals (for example, parallelogram, rhombus, trapezium). Pupils compare and order angles in preparation for using a protractor and compare lengths and angles to decide if a polygon is regular or irregular.

Pupils draw symmetric patterns using a variety of media to become familiar with different orientations of lines of symmetry; and recognise line symmetry in a variety of diagrams, including where the line of symmetry does not dissect the original shape.

**Geometry-position and direction**

Pupils draw a pair of axes in one quadrant, with equal scales and integer labels. They read, write and use pairs of coordinates, for example (2, 5), including using coordinate-plotting ICT tools.

**Statistics**

 Pupils understand and use a greater range of scales in their representations. Pupils begin to relate the graphical representation of data to recording change over time